

## Homework 5: Due Friday 10/12/18

Name: Me

## BLC150-Algebra Workshop

**Exercise 5.1a:** Multiply out the following and simplify when possible [Mostly distribution.]

E.g. $3x(x - y) = 3x^2 - 3xy$	a) $5(x + 2y) =$ $5x + 10y$
b) $2x(x + y) =$ $2x^2 + 2xy$	c) $(x - y)3x =$ $3x^2 - 3xy$
d) $r(-3 + x) =$ $-3r + rx \text{ or } rx - 3r$	e) $r^3(x - 3) =$ $r^3x - 3r^3$

**Exercise 5.1b:** Factor out the Greatest Common Factor.

E.g. $3x^2 - 3xy = 3x(x - y)$	f) $2x^2 + 2xy =$ $2x(x + y)$
g) $r^3x - 3r^3 =$ $r^3(x - 3)$	h) $rx - 3r =$ $r(x - 3)$
i) $3x^2 - 3xy - 3 =$ $3(x^2 - xy - 1)$	j) $5x + 10y =$ $5(x + 2y)$
k) $10x^2 - 12xy - 2x =$ $2x(5x - 6y - 1)$	l) $10x^8 + 20x^4 - 40x^2y^2 =$ $10x^2(x^6 + 2x^2 - 4y^2)$

**Exercise 5.2a:** Using FOIL, multiply these quadratics out and simplify to the form  $x^2 \pm bx \pm c$ .

E.g. $(x + 2)(x - 5) = x^2 - 3x - 10$	a) $(x + 3)(x - 3) =$ $x^2 - 3x + 3x - 9 = x^2 - 9$
b) $(x + 4)(x + 5) =$ $x^2 + 5x + 4x + 20 = x^2 + 9x + 20$	c) $(x - 7)(x + 7) =$ $x^2 + 7x - 7x - 49 = x^2 - 49$
d) $(4 + x)(x + 5) =$ $4x + 20 + x^2 + 5x = x^2 + 9x + 20$	e) $(x + 7)(x + 7) =$ $x^2 + 7x + 7x + 49 = x^2 + 14x + 49$
f) $(x - 4)(x - 5) =$ $x^2 - 5x - 4x + 20 = x^2 - 9x + 20$	g) $(x + y)(x - y) =$ $x^2 - xy + xy - y^2 = x^2 - y^2$
h) $(4 - x)(5 - x) =$ $20 - 4x - 5x + x^2 = x^2 - 9x + 20$	i) $(x + 6)(x - 6) =$ $x^2 - 6x + 6x - 36 = x^2 - 36$
j) $(-x + 4)(-x + 5) =$ $x^2 - 5x - 4x + 20 = x^2 - 9x + 20$	k) $(x + 6)(x + 6) =$ $x^2 + 6x + 6x + 36 = x^2 + 12x + 36$

**Exercise 5.2b:** Factor these quadratics into the form  $(x \pm a)(x \pm b)$ . Use scrap paper if necessary.

E.g.1)  $x^2 - 3x - 10 = (x + 2)(x - 5)$

E.g.2)  $x^2 - 81 = (x + 9)(x - 9)$

m)  $x^2 + 9x + 20 =$   $(x \pm ?)(x \pm ?)$   
 $5 \cdot 4 = 20$  }  $(x + 5)(x + 4)$   
 $5 + 4 = 9$  }

o)  $x^2 - 9x + 20 =$   $(x \pm ?)(x \pm ?)$   
 $-5 \cdot (-4) = 20$  }  $(x - 5)(x - 4)$   
 $-5 + (-4) = -9$  }

q)  $x^2 + 12x + 36 =$   $(x \quad )(x \quad )$   
 $6 \cdot 6 = 36$  }  $(x + 6)(x + 6) = (x+6)^2$   
 $6 + 6 = 12$  }

s)  $x^2 + 14x + 49 =$   $(x+7)^2$   
 $7 \cdot 7 = 49$  }  
 $7 + 7 = 14$  }

u)  $2x^2 + 18x + 40 =$   $2(x^2 + 9x + 20)$   
 $2(x+5)(x+4)$

Hint: Factor out the Greatest Common Factor first, then proceed.

l)  $x^2 - 36 =$   $(x + 6)(x - 6)$   
 $6 \cdot (-6) = -36$

n)  $x^2 - 49 =$   $(x + 7)(x - 7)$   
 $7 \cdot (-7) = -49$

p)  $x^2 - 9 =$   $(x + 3)(x - 3)$   
 $3 \cdot (-3) = -9$

r)  $x^2 - y^2 =$   $(x+y)(x-y)$   
 $y \cdot (-y) = -y^2$

t)  $10x^2 - 90 =$   $10(x^2 - 9) = 10(x+3)(x-3)$   
 Hint: Factor out a 10 first. The final form will be  $10(x-?)(x+?)$

v)  $x^2 + 2x + 1 =$   $(x+1)(x+1) = (x+1)^2$   
 $1+1=2$  }