

Homework 10- Quadratic Equations and Graphs, pt. I

*The Ur quadratic:  $y = x^2$*

$y = x^2$	
$x$	$y$
0	0
1	1
2	4
3	9
-1	1
-2	4
-3	9
1/2	1/4
-1/2	1/4

With the advent of computers, a new notation for exponents has come into fashion:  $x^2 = x^{\wedge}2$ . That little hat is shift-6. E.g.  $x^5 = x^{\wedge}5$ .

Plot some points. Choose some easy values for  $x$  and evaluate the  $y$ .

If  $x = 0$ , then  $y = 0$

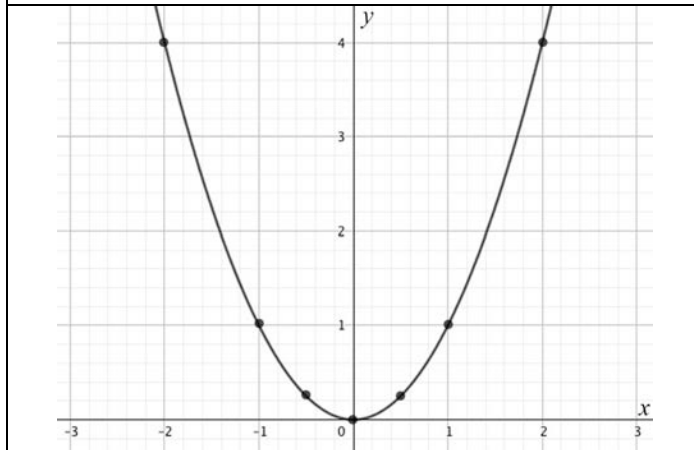
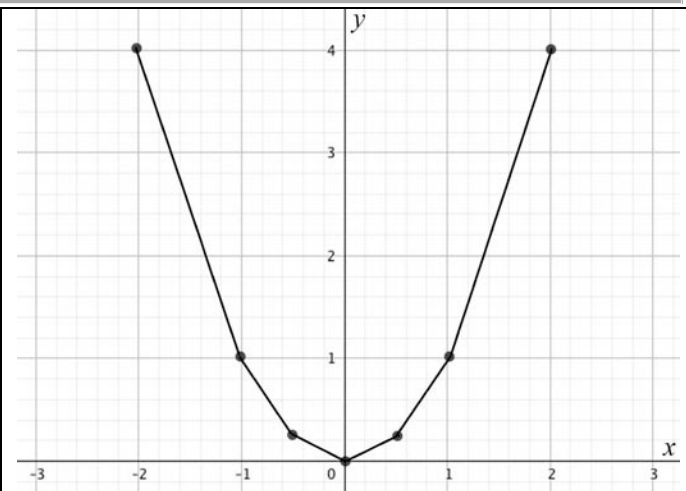
If  $x = 1$ , then  $y = 1$

If  $x = -1$ , then  $y = 1$ , because  $-1(-1) = 1$

If  $x = 2$ , then  $y = 4$ .

If  $x = -2$ , then  $y = 4$ , etc.

Now plot those points on a graph and connect the dots.

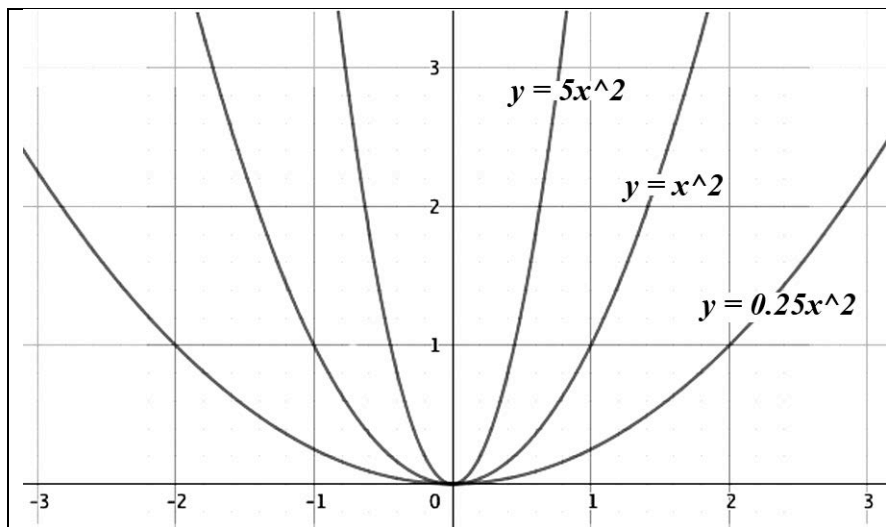
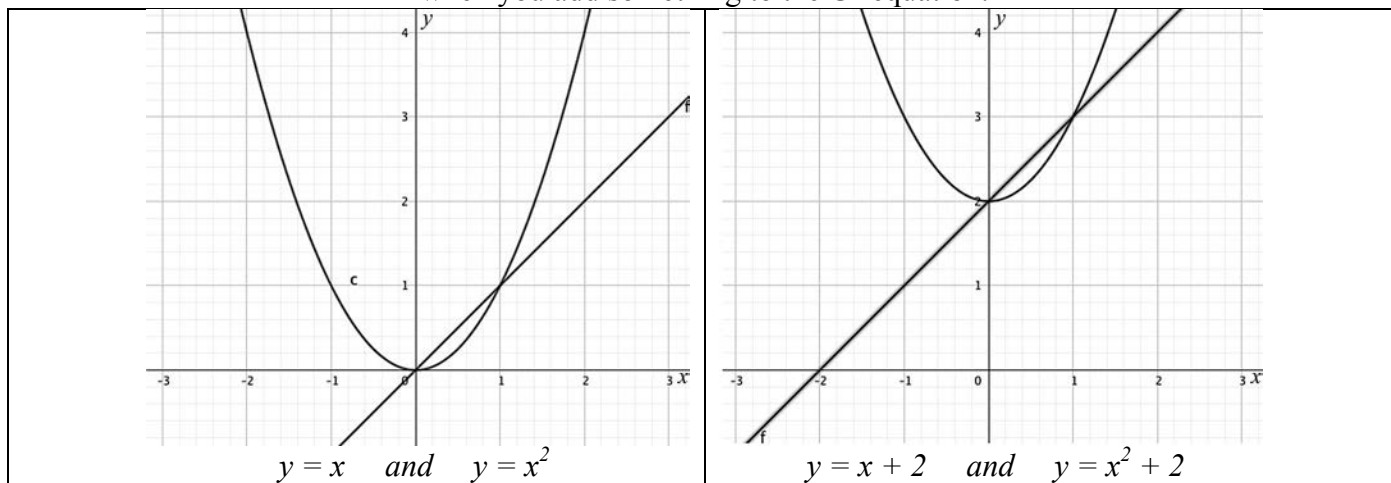


$y = x^2$	
$x$	$y$
0.00	0
0.25	0.0625
0.50	0.25
0.75	0.5625
1.00	1
1.25	1.5625
1.50	2.25
1.75	3.0625
2.00	4

If you calculate a lot more dots, the graph will smooth out.

A computer graphing program is handy. I personally like GeoGebra: <https://www.geogebra.org/?lang=en>  
 It's free and easy to use. It can work without a link to the internet. I put a link on the web site. I suggest you get it and play around with it when you do homework.

Like linear equations, quadratic equations move up and down when you add something to the Ur equation.



In a linear equation a slope makes it steeper.  $y = 5x$  is a steep slope. In a quadratic equation a similar concept isn't called slope, but it makes the parabola tighter. The higher the number, the more the curve tightens up.

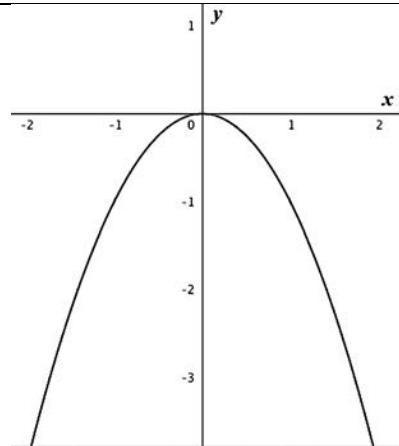
And a negative "quadratic slope" flips the smile over to a frown.

**If the  $x^2$  term is positive, then a smile.**

**If the  $x^2$  term is negative, then a frown.**

To the right is a graph of  $y = -x^2$  Sad. [ $y = -x^2$ ]

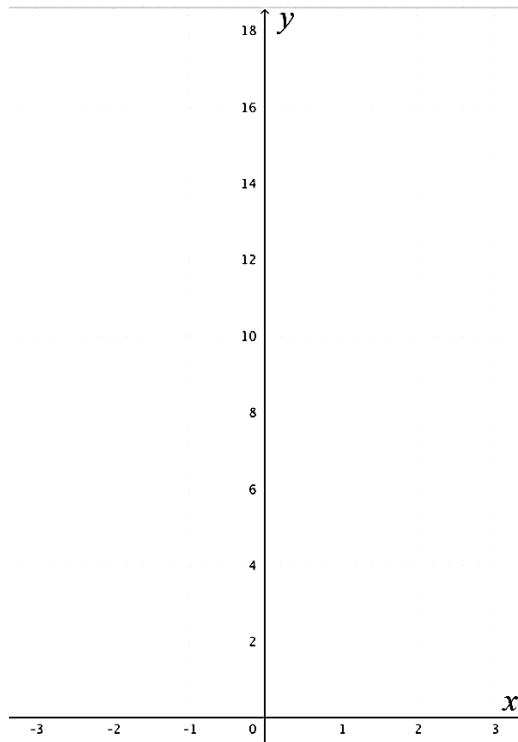
*[The ones above are all happy.]*



### Exercise 9

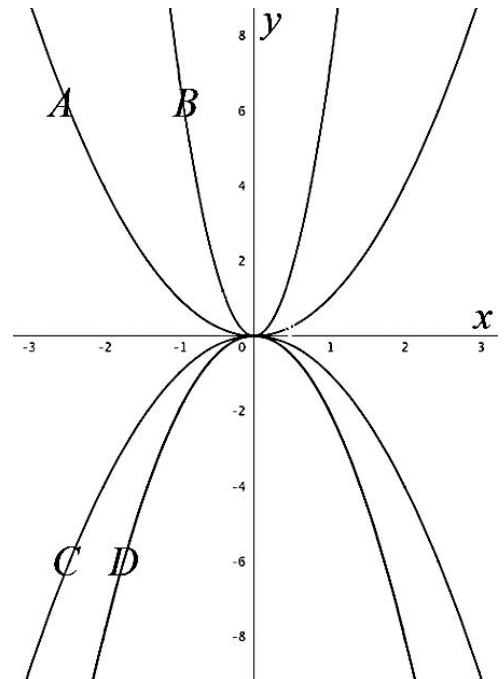
1. Plot the following points for the quadratic equation,  $y = 2x^2$ . Then connect the dots smoothly.

$y = 2x^2$	
$x$	$y$
0	
1	
-1	
2	
-2	
3	
-3	



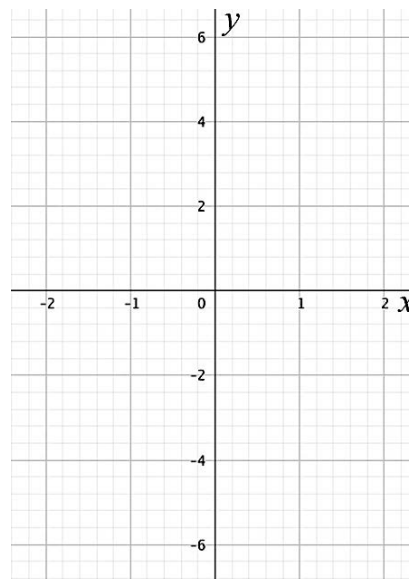
2. Identify which equation goes with which graph.

	Choose, A, B, C, or D. Refer to the graph.
$y = 7x^2$	
$y = x^2$	
$y = -x^2$	
$y = -2x^2$	



3. Graph the following two quadratic equations on the graph.

a.  $y = 2x^2 - 2$       b.  $y = -2x^2 + 2$



Just like in linear equations, you find the *y-intercepts* by setting  $x = 0$ .

Find the *y-intercepts* for the following.


Just solve for  $x = 0$ . Easy.

E.g. $y = 3.5x^2 - 8$	<i>y-intercept</i> is $-8$
1. $y = 4x^2 - 16$	
2. $y = x^2 + 16.3$	
3. $y = -3.5x^2 - 8$	
4. $y = 0.002x^2 + 7$	
5. $y = x^2$	

Find the *x* and *y-intercepts* for the following.

The *x-intercepts* are much trickier.

You set  $y = 0$  and solve for  $x$ .

	<i>x-intercepts</i>	<i>y-intercept</i>	<i>Happy or Sad</i>
E.g. $y = 4x^2 - 16$ $0 = 4x^2 - 16$ $16 = 4x^2$ $x^2 = 4$ $x = \pm 2$	<i>x-intercept</i> is $-2$ and $+2$ .  <i>See the graph</i> <i>to the right.</i>	$-16$	<i>Happy</i> $0 \ 0$  <i>Because the <math>x^2</math> term is positive.</i>
6. $y = x^2 - 4$			
7. $y = -x^2 + 4$			<i>Sad</i>
8. $y = -3x^2 + 27$			
9. $y = 2x^2 - 18$			
10. $y = x^2$			

